

For Problems 31-35, see the Mathematica .nb files for details.

12a

31) Critical numbers:  $x = \frac{(5/3)^{2/5}}{2^{4/5}} \approx 0.704556$  Absolute Max  
+ Local Max

$x \approx 1.74364$  Absolute Min + Local Min

End Points:  $x=0$  Local Min

$x=2$  Local Max

Note: I am able to classify these by viewing the graph in Mathematica.  
That is how I do all 4 of the next problems.

$$f(0) = 16$$

$$f(0.7046) = 56.2$$

$$f(1.74364) = 1.5 \times 10^{-9} \leftarrow \text{This is not 0 because of round off error. If we used more digits in the } 1.74\dots \text{ part we would get zero here.}$$

$$f(2) = (-12 + 5\sqrt{2})^2 \approx 24.3$$

Note: The "//N" in the Mathematica file forces the output to be a numerical answer (i.e. 1.4142... instead of  $\sqrt{2}$  or 3.14159... instead of  $\pi$ )

Note: The  $i$  symbol in Mathematica indicates a Complex (not Real) number. We ignore those critical numbers.

32) Critical numbers:  $x = -4.03749$  Local Max + Absolute Max  
 $x = -0.95933$  Local Min  
 $x = 1.0521$  Local Max  
 $x = 2.94473$  Local Min

Endpoints:  $x = -6$  Absolute Min + Local Min  
 $x = 4$  Local Max

$f(-6) = -1836/5 = -367.2$   
 $f(-4.03) = 88.6$   
 $f(-0.9593) = -7.63689$   
 $f(1.0321) = 8.1428$   
 $f(2.944) = -12.23$   
 $f(4) = 592/5 = 39.47$

33) Critical Numbers  $x = 16/19 \approx .842$  X Not in range we consider in this problem

$f(4) = 0$   
 $f(2) = -13.9$   
 $f(6) = 33.5$

$x = 4$  Neither a max nor min.  
 Note that  $f'(x)$  does not change sign at  $x = 4$ .

End Points  $x = 2$  Absolute + Local Min  
 $x = 6$  Absolute + Local Max

34) Critical Points  $x = -3$  Local Min + Absolute Min  
 $x = 0$  Neither Max nor Min ( $f'(x)$  does not cross the x-axis at  $x = 0$ )  
 End Points  $x = -4$  Local Max  
 $x = 2$  Local Max

$f(-3) = -1.344$   
 $f(0) = 0$   
 $f(-4) = -1.722$   
 $f(2) = 59.11$

Note: Instead of "//N" you can use a decimal point to ask mathematicians for the decimal representation of your answer. For example, try  $f[2]$  vs.  $f[2.]$  or  $f[2.0]$

35) Critical Numbers  $x = 0.664751$  Local Max  
 $x = 0.824935$  Local Min  
 $x = 0.939484$  Local Min  
 $x = 1.07166$  Local Min  
 $x = 1.40921$  Local Max + Absolute Max  
 $x = 1.51047$  Local Min  
 $x = 1.55872$  Local Max

End Points  $x = 0$  Local Min + Absolute Min  
 $x = \pi/2 = 1.57...$  Local Min

$f(0.664751) = 2.93747$   
 $f(0.824935) = 2.54239$   
 $f(0.939484) = 2.76393$   
 $f(1.07166) = 2.2359$   
 $f(1.40921) = 5.21567$   
 $f(1.51047) = 4.55689$   
 $f(1.55872) = 4.65191$   
 $f(0) = 0$   
 $f(\pi/2) = 4.63271$